Research Experience for Undergraduates Summer School on Mathematical Foundation of Data Science

June 2, 2025 --- July 11, 2025

LeConte 101 Department of Mathematics University of South Carolina

or

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Sponsored by: Department of Mathematics University of South Carolina

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Organized by:

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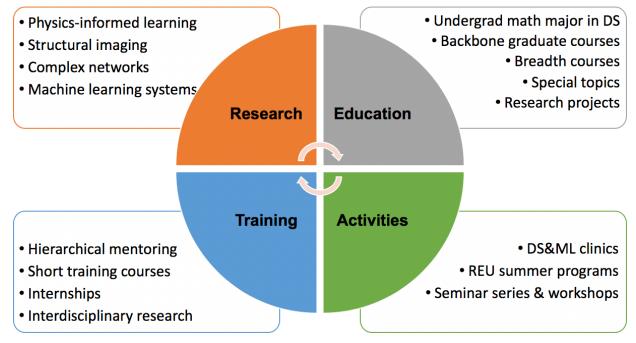




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Section 1: Program Overview

This REU summer program is part of the NSF RTG project **"RTG: Mathematical Foundation of Data Science at University of South Carolina"**, which aims to develop a multi-tier Research Training Program at the University of South Carolina (UofSC) designed to prepare the future workforce in a multidisciplinary paradigm of modern data science. The education and training models will leverage knowledge and experience already existing among the faculty and bring in new talent to foster mathematical data science expertise and research portfolios through a vertical integration of post-doctoral research associates, graduate students, undergraduate students, and advanced high school students. A primary focus of this project is to recruit and train U.S. Citizens, females, and underrepresented minority (URM) among undergraduate and graduate students, and postdocs through research led training in Data Science.



For more information on the NSF RTG project, please visit us at the following URL: https://sc.edu/study/colleges_schools/artsandsciences/mathematics/my_mathematics/rtg/index.php. The REU summer program of this year runs in-person and virtually from June 6 to July 15. Starting from the first week, students will be divided into several groups to work on research projects. Some guest speakers are invited to give talks on the latest development in the Mathematical Foundation of Data Science. On the last day of the program, students will present their research findings.

Section 2: Research Projects (Tp be edited by Faculty Advisor)

2.1 Developing AI tools for Scanning Tunneling Microscopy (STM) (Advisor: Peter Binev)

Scanning Tunneling Microscopy (STM) is used to observe the atomic structure of the surface of the materials. Data acquisition tasks in STM usually require a human-in-the-loop component to constantly evaluate the structural phenomena on the surface and navigate towards the ones of interests. Using AI to take care of most of these evaluations would allow a rapid increase in materials research. The first step in achieving this is the development of data processing tools and deep learning routines to recognize the usual structures and classify them. The research project involves investigating and training deep learning autoencoders to extract pattern information from artificial and real data, as well as using this information to advance different image processing tasks.

Further information about the research area can be found in last year's project report https://arxiv.org/pdf/2501.13283.

2.2 AI Tools for Digital Twins for Health (Advisor: Qi Wang)

Biomedical applications are ideal implementation venues for AI models and tools. With AI integration, biomedical research and healthcare deliveries could experience a transformational change. The project goal is to develop biomedical AI models, data processing and computational infrastructures to support the development and implementation of AI-enabled digital twins for health in the form of software. Several fundamental theories/foundation models, methods, and tools are developed to facilitate research projects in this area. The REU component will include adding front-end user-interfaces for some basic models for specific diseases so that the models can be used in the clinical setting. The three major tasks in the current digital twin project consist of data imputation and synthetic data generation, multiclass classification, and time-series forecasting. The student will work with the existing research group to implement the already developed models and modules. New models may be developed for enhance the existing digital twin platform.

2.3 From Language to Action: Distributed LLM-Based Robot Control and Planning (Advisor: Pooyan Jamshidi)

The topic I would like you to explore would be the synergy between LLM and Robotics. Specifically, task planning and execution by:

- Translating natural language commands into robot actions,
- Multi-modal task planning using visual and textual information.

To achieve the above, we would explore distributed LLM strategy. This distributed framework would be the outcome of your internship by demonstrating: (i) a robot will go to a location, (ii) a manipulator will pick and place an object, and (iii) combination of (i) and (ii), by taking natural language command. Example natural language command: "Robot, go

to the kitchen and bring the coffee mug from the coffee machine to the living room table if there is coffee in the mug."

The project would be mostly developing a unified software. We may use technologies such as Ollama, Cake, ROS, Python. The goal would be to make the framework software and hardware agnostic. For this, we may implement APIs using Flask.

2.4 Spatiotemporal Modeling for Disease Mapping and Causal Inference

(Advisor: Ray Bai)

A critical task in public health is disease mapping, which aims to analyze the distribution and spread of diseases across time and space. This can help epidemiologists and policymakers to identify disease patterns and predict areas that are at elevated risk of future outbreaks. Bayesian spatiotemporal modeling is widely used in practice for disease mapping. In addition to predicting disease prevalence, these models also help policymakers to identify county-level characteristics (e.g. percentage of residents who are uninsured) that are highly associated with disease prevalence. However, association does not imply causation. If we want to study whether a particular county-level characteristic *causes* disease prevalence to either increase or decrease, then we need to bring in causal inference.

In this project, participants will use Bayesian spatiotemporal models to predict disease prevalence of a disease of their choice (e.g. an infectious disease or a chronic disease) at the county level in the United States. If time allows, we will also extend the model to infer the causal effect of a treatment on the disease prevalence.

2.5 Simulating Transport and Diffusion in Physical and Biological Systems (Advisor: Changhui Tan/Siming He)

This REU project explores how transport (directed movement) and diffusion (random spreading) interact in systems governed by partial differential equations (PDEs). Such models arise in many contexts. For example, to describe the spread of biological populations (Fisher-KPP equations) or the phase separation of materials (Allen-Cahn equation).

However, when external transport effects are incorporated, the qualitative behavior of solutions can change substantially, influencing the speed of propagation, pattern formation, and solution stability. Students will develop MATLAB code to simulate the PDEs numerically. The project involves:

- Learning basic PDE knowledge about the transport and diffusion phenomena;
- Developing numerical schemes to solve these equations;

• Running numerical experiments to explore how transport modifies diffusion-driven behavior. This project suits students interested in scientific computing, numerical modeling, and applying data-driven approaches to real-world systems.

2.6 - Ricci Curvature on Graphs (Advisor: Linyuan Lu)

Throughout the last thirty years, extensive efforts have been made to adapt the concept of Ricci curvature from Riemannian geometry to a discrete framework. This adaptation enables the treatment of graphs similarly to manifolds. Curvature has been applied in various research areas such as network analysis, quantum computation, dynamic Networks, etc. In this project, we aim to explore the characteristics of graphs exhibiting positive Lin-Lu-Yau Ricci curvature.

Section 3: Program Calendar

D	ay	Activity	Moderator
Monday	9:00-12:00	Introduction to the REU program	
June 2	12:00-2:00	Lunch break	
5 dile 2	2:00-5:00	Group assignments	
Tuesday	9:00-12:00	Parallel research sessions	
June 3	12:00-2:00	Lunch break	
June J	2:00-5:00	Parallel research sessions	
Wadnasday	9:00-12:00	Parallel research sessions	
Wednesday June 4	12:00-2:00	Lunch break	
t une 1	2:00-5:00	Parallel research sessions	
Thursday	9:00-12:00	Parallel research sessions	
Thursday June 5	12:00-2:00	Lunch break	
	2:00-5:00	Parallel research sessions	
	9:00-10:30	Parallel research sessions	
Friday	10:30-12:00	Group presentation	
June 6	12:00-2:00	Lunch break	
	2:00-5:00	Social/free time	

Week 1

Week 2

Γ	Day	Activity	Moderator
Monday	9:00-12:00	Parallel research sessions	
June 9	12:00-2:00	Lunch break	
June y	2:00-5:00	Parallel research sessions	
Tuesday	9:00-12:00	Parallel research sessions	
June 10	12:00-2:00	Lunch break	
suite 10	2:00-5:00	Parallel research sessions	
Wednesday	9:00-12:00	Parallel research sessions	

June 11	12:00-2:00	Lunch break
	2:00-5:00	Parallel research sessions
TI 1	9:00-12:00	Parallel research sessions
Thursday June 12	12:00-2:00	Lunch break
	2:00-5:00	Parallel research sessions
	9:00-10:30	Parallel research sessions
Friday June 13	10:30-12:00	Group presentation
	12:00-2:00	Lunch break
	2:00-5:00	Social/free time

Week 3

E	Day	Activity	Moderator
Mandana	9:00-12:00	Parallel research sessions	
Monday June 16	12:00-2:00	Lunch break	
	2:00-5:00	Parallel research sessions	
Tuesday	9:00-12:00	Parallel research sessions	
June 17	12:00-2:00	Lunch break	
suno 17	2:00-5:00	Parallel research sessions	
Wednesday	9:00-12:00	Parallel research sessions	
June 18	12:00-2:00	Lunch break	
vane 10	2:00-5:00	Parallel research sessions	
Thursday	9:00-12:00	Parallel research sessions	
Thursday June 19	12:00-2:00	Lunch break	
	2:00-5:00	Parallel research sessions	
	9:00-10:30	Parallel research sessions	
Friday	10:30-12:00	Group presentation	
June 20	12:00-2:00	Lunch break	
	2:00-5:00	Social/free time	

Week 4

D	ay	Activity	Moderator
Mandary	9:00-12:00	Parallel research sessions	
Monday June 23	12:00-2:00	Lunch break	
June 25	2:00-5:00	Parallel research sessions	
Tuesday	9:00-12:00	Parallel research sessions	
June 24	12:00-2:00	Lunch break	
June 21	2:00-5:00	Parallel research sessions	
Wednesday	9:00-12:00	Parallel research sessions	
June 25	12:00-2:00	Lunch break	
	2:00-5:00	Parallel research sessions	

Thursday June 26	9:00-12:00	Parallel research sessions
	12:00-2:00	Lunch break
	2:00-5:00	Parallel research sessions
Friday June 27	9:00-10:30	Parallel research sessions
	10:30-12:00	Group presentation
	12:00-2:00	Lunch break
	2:00-5:00	Social/free time

Week 5

E	Day	Activity	Moderator
	9:00-12:00	Parallel research sessions	
Monday June 30	12:00-2:00	Lunch break	
June 30	2:00-5:00	Parallel research sessions	
Turadari	9:00-12:00	Parallel research sessions	
Tuesday July 1	12:00-2:00	Lunch break	
July I	2:00-5:00	Parallel research sessions	
XX 1 1	9:00-12:00	Parallel research sessions	
Wednesday July 2	12:00-2:00	Lunch break	
July 2	2:00-5:00	Parallel research sessions	
	9:00-10:30	Parallel research sessions	
Thursday	10:30-12:00	Group presentation	
July 3	12:00-2:00	Lunch break	
	2:00-5:00	No activities	
Friday July 4	Holiday	No activities	

Week 6

D	Day	Activity	Moderator
Monday	9:00-12:00	Parallel research sessions	
July 7	12:00-2:00	Lunch break	
July /	2:00-5:00	Parallel research sessions	
Tuesday	9:00-12:00	Parallel research sessions	
July 8	12:00-2:00	Lunch break	
Sury 0	2:00-5:00	Parallel research sessions	
Wednesday	9:00-12:00	Parallel research sessions	

July 9	12:00-2:00	Lunch break	
	2:00-5:00	Parallel research sessions	
771 1	9:00-12:00	Parallel research sessions	
Thursday July 10	12:00-2:00	Lunch break	
oury ro	2:00-5:00	Parallel research sessions	
	9:00-10:30	Parallel research sessions	
Friday	10:30-12:00	Joint research sessions	
July 11	12:00-2:00	Lunch break	
	2:00-5:00	Final presentations and group photo	

Section 4: Contact Information

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